JAWAHARLAL NEHRU TECHNOLOGICAL UNIVERSITY HYDERABAD B.Tech I Year Examinations, June - 2022

MATHEMATICS - I

(Common to CE, EEE, ME, ECE, CSE, IT, AE, AME, MIE)

Time: 3 Hours

Max. Marks: 75

Answer any five questions All questions carry equal marks

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- 1.a) Test for convergence of the series $u_n = \frac{n^2 n + 1}{n!}$
 - b) Prove that the series is $\frac{1}{2^3} \frac{1}{3^3} (1+2) + \frac{1}{4^3} (1+2+3) \frac{1}{5^3} (1+2+3+4)$ ∞ conditionally convergent. [6+9]
- 2.a) Verify Rolle's theorem for $f(x) = \frac{\sin x}{e^x}$ in $(0, \pi)$.
 - b) A rectangular box open at the top is to have volume of 32 cubic ft. Find the dimensions of the box requiring least material for its construction. [6+9]
- 3.a) Find the radius of curvature at the point $\left(\frac{3a}{2}, \frac{3a}{2}\right)$ on the curve $x^3 + y^3 = 3axy$.
 - b) Find the envelope of the family of curves $y = mx + \sqrt{a^2m^2 + b^2}$; m is a parameter. [9+6]
- 4.a) Evaluate $\int_{0}^{a} \int_{0}^{\sqrt{a^2 x^2}} (x^2 y + y^3) dx dy$.
 - b) Evaluate by changing the order of integration $\int_0^\infty \int_x^\infty \frac{e^{-y} dy}{y} dx$. [7+8]
- 5.a) Solve the differential equation $y(xy + e^x)dx e^x dy = 0$.
 - b) Find the Orthogonal Trajectories of the family of curves $x^2 + y^2 = ax$. [8+7]
- 6.a) Solve the differential equation $(D^2 + D + 1)y = x^3$.
 - b) Solve the differential equation $(D^2 + 5D + 6)y = e^{-3x}$. [8+7]
- 7.a) Find L[$(t^2 + 1)^2$].
 - b) Find Inverse Laplace transform of $\frac{3s+7}{(s^2-2s-3)}$. [6+9]
- 8.a) Find a unit normal vector to the surface $x^3 + y^3 + z^3 = 3$ at the point (1,-2,1).
 - b) Applying, Green's theorem evaluate $\oint_C (y \sin x) dx + \cos x dy$ where C is the plane triangle enclosed by the lines $y = 0, x = \frac{\pi}{2}$ and $y = \frac{2x}{\pi}$. [6+9]